

INTEGRATION OF ECONOMIC PRODUCTION QUANTITY WITH DEFECTIVE ITEMS FOR MULTI-PRODUCT IN MULTI-PERIOD

GEETHAMPARI A/P SUBAMANIAM

UNIVERSITI TEKNOLOGI MALAYSIA

INTEGRATION OF ECONOMIC PRODUCTION QUANTITY WITH
DEFECTIVE ITEMS FOR MULTI-PRODUCT IN MULTI-PERIOD

GEETHAMPARI A/P SUBAMANIAM

A thesis submitted in fulfilment of the
requirements for the award of the degree of
Master of Science (Mathematics)

Faculty of Science
Universiti Teknologi Malaysia

OCTOBER 2017

To my beloved family for their never ending support and care

ABSTRACT

Manufacturers often face material losses during the process of any specific production assemblies which are usually unpredictable. However, the attrition percentage can normally be obtained. In order to make sure that the demand is met despite attrition, the production needs to be planned wisely. Inefficient production planning can lead to the consumption of capital resources that can otherwise be put into better use elsewhere in the company. In this study, an inventory model that takes attrition into consideration with no shortage allowed is developed. An Economic Production Quantity with Attrition (EPQA) model is used to obtain the optimal production run size and the optimal production cycle. Then, an aggregate planning model for five periods of time is developed taking the optimal production run size obtained as the demand. This model will help the decision making process by determining the production quantity of products, use of overtime labor, number of workers to be hired or fired and the amount of inventory to be held in stock each period so that the demand is met and the annual total cost of operations is kept to the minimum. This new production policy can thus scientifically address the attrition problem, assist in decision making, help in resource planning and optimize the production process. For future study, the attrition could be included as an inherent parameter in material or inventory planning to make sure that required materials are sufficient to satisfy demands even when attritions exist.

ABSTRAK

Pengilang sering menghadapi kekisiran ketara semasa proses mana-mana pemasangan pengeluaran tertentu dimana kebiasannya adalah tidak dapat diramalkan. Walau bagaimanapun, peratusan keciciran selalunya boleh diperolehi. Dalam usaha untuk memastikan bahawa permintaan bahan dipenuhi walaupun keciciran berlaku, pengeluaran perlu dirancang dengan bijak. Perancangan pengeluaran yang tidak cekap boleh membawa kepada penggunaan sumber modal yang sepatutnya lagi baik digunakan oleh bahagian lain dalam syarikat. Dalam kajian ini, model inventori yang mengambil kira keciciran tanpa membenarkan sebarang kekurangan telah dibangunkan. Satu model Pengeluaran Kuantiti Ekonomi dengan keciciran (EPQA) digunakan untuk mendapatkan saiz pengeluaran optimum dan kitaran pengeluaran yang optimum. Kemudian, satu model perancangan agregat untuk lima tempoh masa dibangunkan mengambil saiz pengeluaran optimum yang diperolehi sebagai permintaan. Model ini membantu proses membuat keputusan dengan menentukan kuantiti pengeluaran produk, penggunaan tenaga buruh lebih masa, bilangan pekerja yang diambil dan dipecat dan jumlah inventori yang akan disimpan dalam stok untuk setiap tempoh masa supaya permintaan dipenuhi dan jumlah kos operasi tahunan ditetapkan pada tahap minimum. Dasar pengeluaran baharu ini boleh menangani masalah keciciran secara saintifik, membantu dalam membuat keputusan, membantu dalam perancangan sumber dan mengoptimumkan proses pengeluaran. Untuk kajian akan datang, keciciran boleh dipertimbangkan sebagai parameter yang ada dalam perancangan bahan atau inventori untuk memastikan bahan-bahan yang mencukupi untuk memenuhi permintaan walaupun keciciran wujud.

TABLE OF CONTENTS

CHAPTER	TITLE	PAGE
	DECLARATION	ii
	DEDICATION	iv
	ACKNOWLEDGEMENT	v
	ABSTRACT	vi
	ABSTRAK	vii
	TABLE OF CONTENTS	viii
	LIST OF TABLES	xiii
	LIST OF FIGURES	xv
	LIST OF SYMBOLS	xvii
	LIST OF APPENDICES	xviii
1	INTRODUCTION	1
	1.1 Overview	1
	1.2 Motivation	3
	1.3 Inventory Accuracy	4
	1.4 Attirition	5
	1.5 Background Research	6
	1.6 Problem Statement	10
	1.7 Research Question	10
	1.8 Research Obejctive	11
	1.9 Scope of the Research	12
	1.10 Significance of the Research	12
	1.11 Organization of Thesis	12

2	LITERATURE REVIEW	14
2.1	Introduction	14
2.2	Optimization in Production Planning	15
2.3	Manufacturing Types	15
2.3.1	Just in Time (JIT)	15
2.3.2	Continuous Production	16
2.4	Inventory Management	16
2.4.1	EPQ & APP in Inventory Management	17
2.5	Birth of EPQ	17
2.5.1	Traditional EPQ	17
2.5.2	Modern EPQ	18
2.5.3	Production Lead Time and Setup Cost in EPQ	18
2.5.4	Imperfect Process in EPQ	19
2.5.5	EPQ Model Formulation	21
2.5.5.1	Example of EPQ Model Application	24
2.6	Aggregate Production Planning (APP)	26
2.6.1	Characteristics of APP	27
2.6.2	APP Strategies	28
2.6.2.1	Level Strategy	28
2.6.2.2	Chase Strategy	29
2.6.3	Related Studies in APP	29
2.6.3.1	Uncertainty in APP	30
2.6.3.2	Integration of APP in Real Situation	33
2.6.3.3	Mathematic Method in APP	33
2.7	LINGO 15.0	36
2.8	Discussion	39
2.9	Summary	40

3	RESEARCH METHODOLOGY	41
3.1	Introduction	41
3.2	Overall Research Plan	41
3.3	Research Design & Procedure	45
3.3.1	Step1: Framing the Questions	46
3.3.2	Step2: Finding Research Gap	46
3.3.3	Step3: Data Collection	47
3.3.4	Step4: Data Analysis	48
3.3.5	Step5: Build EPQA and APP model	48
3.3.6	Step6: Running & Testing Model	49
3.3.7	Step7: Interpreting the Results	49
3.3.8	Step 8: Sensitivity Analysis	49
3.4	Theoretical Framework	49
3.5	Summary	52
4	EPQA MODEL DEVELOPMENT AND SOLUTION ANALYSIS	53
4.1	Introduction	53
4.2	Problem Description	53
4.3	Mathematical Model Formulation	55
4.3.1	Notation	55
4.3.2	Assumption	56
4.3.3	Modelling with Attrition and Shortage Not Allowed	56
4.4	Model Implementation and Numerical Analysis	60
4.5	Conclusion	70

6	CONCLUSION AND RECOMMENDATION	108
	6.0 Overview	108
	6.1 Summary	108
	6.2 Conclusion	110
	6.3 Recommendation for Future Research	111
	REFERENCES	112
	Appendices A - L	119

LIST OF FIGURES

FIGURE NO.	TITLE	PAGE
1.1	Flowchart of Problem Formulation	9
2.1	Operation Planning Hierarchy (Chinguwa, 2013)	31
2.2	Example of LINGO 15.0 Interface	37
2.3	Example of LINGO 15.0 Solver Status Box	38
2.4	Example of LINGO 15.0 Solution Report	39
3.1	Operational Framework of Research	50
3.2	Theoretical Framework of Research	51
4.1	Behaviour Of Inventory Level Over Time	57
5.1	Solver Status Window: Scenario 1	83
5.2	Solver Status Window: Scenario 2	87
5.3	Solver Status Window: Scenario 3	90
5.4	Solver Status Window: Scenario 4	94
5.5	Solver Status Window: Scenario 5	98
5.6	Solver Status Window: Scenario 6	102

LIST OF SYMBOLS

p_i	-	Daily replenishment or production rate at product i
r_i	-	Daily demand rate at product i
R_i	-	Annual demand in units
m	-	Number of annual orders or production runs
t_p	-	Transit time in years for replenishment order
P	-	Production cost
C	-	Setup cost
H_i	-	Holding cost per unit for product i
$TC(m)$	-	Total annual cost for m production runs per year
Q_i	-	Lot size for product i
N	-	Number of annual operating days
$_{ik}$	-	Production rate
$x_{\#}$	-	inventory level
k	-	wo

LIST OF APPENDICES

APPENDIX	TITLE	PAGE
A	LINGO Model : Scenario 1	119
B	LINGO Solution Report : Scenario 1	123
C	LINGO Model : Scenario 2	128
D	LINGO Solution Report : Scenario 2	132
E	LINGO Model : Scenario 3	137
F	LINGO Solution Report : Scenario 3	141
G	LINGO Model : Scenario 4	146
H	LINGO Solution Report : Scenario 4	150
I	LINGO Model : Scenario 5	157
J	LINGO Solution Report: Scenario 5	161
K	LINGO Model: Scenario 6	167
L	LINGO Solution Report: Scenario 6	172

CHAPTER 1

INTRODUCTION

1.1 Overview

Production planning in manufacturing is the planning for smooth and optimum production in the company. It utilizes manufacturing resources, material availability and production capacity to serve customers. Production planning is a plan for future production. Quantity of manufacturing resources needed are determined and arranged. A production planning is made periodically for a specific time called horizon. To develop an efficient production planing, the production planner is required to work closely with sales department. A critical factor for production planning is the accurate estimation of the productive capacity of available resources. A production planner also considers material availability, resources availability and future demand.

Economic Production Quantity (EPQ) is a strategy widely used in production planning practice because of its simplicity. Basic EPQ applies when demand of the product is constant over the year and there is fixed cost charged for each product produced regardless of the number of units produced (Hsu, 2014). There is also a holding cost for each unit stored in storage. Recently research efforts have been made to extend the basic EPQ by relaxing the assumptions so that the model conforms more closely to real world problems. There are two major assumptions

the classical EPQ model these are 1) the quality of output is of perfect quality and 2) the production rate is predetermined and fixed in advance.

Aggregate production planning (APP) model is a production planning activity. An APP for the production process is normally done in advance of 2 to 18 months to give an idea to the management as to what quantity of materials to be ordered and when the products should be produced in order to minimize the total cost of the production over that period.

The concept of APP is to translate the forecasted demand and production capacity to future manufacturing plan for a family of products. APP greatly reduced the amount of data used during planning process and also the frequency of revising the plan (Baykasoglu, 2001). The common APP objectives are minimizing cost, minimizing inventory level, minimizing changes in work force level, minimizing use of overtime, minimizing use of subcontracting, minimizing changes in production rate, minimizing number of machine setups and maximizing profits. The research development in APP involves the consideration of multi-objective function, multi-product, multi-period, multi-demand and multi-safety stock.

Both EPQ and APP models involve different implementation in manufacturing. Firstly, EPQ provides information on lot size that need to be run based on demand, production rate, setup cost and inventory cost. On the other hand, Secondly, APP determine amount of product, inventory and workforce level to meet demand requirements over a planning horizon. Demand is an important input in both APP and EPQ.

Attrition is throw out process of raw material during manufacturing process. The throw out of raw material for manufactured products are unpredictable. The amount of raw material which has been loss is not sufficient for next production batch thus the planner required to order those material or stock more to ensure there is no stopper for production. However, this situation leads to high inventory because the attrition quantity is unpredictable.

1.2 Motivation

Demand planning and inventory control are the most important operation activities in manufacturing and require management at its best. The demand data, inventory aging data, inventory analysis in each location are used to justify the order quantity and safety stock in production planning. Economic production quantity is important because holding too much inventory is costly and holding low stock can incur stockouts, lost sales, and in some cases production plan shutdown.

EPQ is designed to help inventory managers maintain the right amount of inventory. EPQ model has been extended by considering the effect of imperfect production process (Porteus, 1986). Practically, imperfect quality items can be sometimes reworked and repaired. AP can be a valuable aid in planning production and workforce levels for a company because it provides a mean of absorbing demand fluctuations by smoothing workforce and production levels.

Inventory inaccuracy may occur due to shortage of materials, imperfect production processes, data input/output errors, transaction errors, cycle count errors and unreported scrap. In addition, attrition where material are discarded during production process, also affects inventory accuracy. This will cause immediate physical shortage to complete the product. Imperfect production process usually happens because of machine errors. This situation is often unavoidable when machines run at high speed. Thus, the planned quantity is not achieved and production tends to use more materials that should be consumed and this also tends to increase production setup cost. This situation causes the planner or purchaser difficulty to bring in materials on time due to extra materials needed earlier than expected to make up for lost production. In some circumstances, production planner tends to project for buffer stocks, but this results in higher inventory on production floor. An inventory model to determine optimal lot size which takes into consideration attritions rate helps the planner to decide on the number of workers and inventory levels to execute the plan.

The influence of demand in APP is significant. Basically demand is a guideline for a planner in meeting customer requirements. Sudden material shortage for the demand due to attrition will have impact on the aggregate production planning done earlier and there is a continuous need to revise the plan again based on current material availability. This will eventually impact customer service level.

1.3 Inventory Accuracy

Some manufacturing plants have no formal policy for reporting and reducing inventory used in subassemblies that must be reworked or scrapped. A detailed investigation is required to determine contribution of the scrap/attrition rate to the inventory inaccuracies. The more complex of the subassembly to be reworked, the more difficult it is to capture the correct materials scrapped or used as replacement. Some subassemblies are so complex that it is difficult to determine what component is scrapped. When the component being reworked is very complex, routine stock adjustment needs to be done or the whole part needs to be scrapped off in the system with any salvagable components placed back on the system. The accuracy of reporting scrap/attrition is a particular area of concern for inventory control.

Operations people may be reluctant to assist in improving scrap reporting since such improvements ultimately may increase the scrap/attrition value in the system reporting. With this situation, there is frequent physical variance and production will have breakdowns on material supply to run production. Material planning is important and critical if attrition is expected in the near to actual planning period.

Another issue in inventory control is the lack of proper control on scraps. Poor or even no reporting of scrap can have major effects on the inventory accuracy. One way is to look at where the scrap is being placed and how it is being processed. The question is "What is the efficient way to do this?" The way it was done may be

considered efficient on the plant. But it was discovered there were some other scrap lots which were not declared and were hidden for a certain period. Even the best system will not be able to give accurate inventory data when there is human interference.

Inventory accuracy is important for APP as it will calculate the material needed based on 6 months or above forecast to ensure production run without any material breakdowns supply. A good system should include the attrition rate with demand loaded in system to sum up total material needed for the production

1.4 Attrition

Attrition refers to the situation when material flows out or is lost during production process. The loss of the materials usually happens when the machine has pick up errors, or when the machines are down. Planner will do planning based on system data on material quantity. If the system shows the quantity is available the model will proceed to production, and production will perform material kitting at sub stores to allocate materials from main store, to run certain planned products. Once production is completed, those materials will be returned to stores and re-count process on the material will be performed. The quantity during re-count may not be the same with the required quantity in the system. This situation creates “attrition”.

In this study, attrition happens mostly for small/tiny parts such as resistors and capacitors which caused physical shortage on next production and product produced as defective. Planners face difficulty to plan if there is unreported attrition, or attrition reported is not done for certain period of time so that the data is out of date. Manufacturing company practice to scrap materials weekly to ensure the inventory data is accurate and alert the planner to purchase those material in short supply immediately.

1.5 Background of Research

EPQ model determines the quantity a company should produce in order to minimize the total production cost. EPQ was developed by Taft in 1918 as an extension of Economic Order Quantity (EOQ) (Taft, 1918). Its fundamental is that the quantity of product should be manufactured in single or multiple batches to ensure total cost is minimized. The cost includes setup costs for machine and inventory holding cost. Thus, total cost of EPQ value should comprise of each cost at its minimum value. This is achieved by differentiating and finding minimum for the equation of the total cost.

A few studies have been done to address the EPQ model with rework. One way is to incorporate the effect of defective items in classical EPQ model (Porteous, 1986). These defective items can be reworked in the same cycle. The author found that optimal EPQ with rework is smaller than classical EPQ and the smaller the defect size, the smaller the defective rate. An optimal result is achieved for finite production model under effect of reworking imperfect quality items if defective items are reworked and repaired (Hayak and Salameh, 2001). A finite production model had been developed with consideration of random defective rate, scrapping and reworking of repairable defective items and backlogging by Chiu (2003). Another study allowed the simultaneous determination of production lot and batch sizes (Buscher and Lindner, 2007). In general, defective item is the product which requires rework or scrap off if unable to rework whereby attrition is the process which produced the defective item. Thus, this research will consider attrition rate in the inventory model to ensure produced product able to meet customer demand.

APP was first conceived in an important series that appeared in the mid 1950s. Holt *et al.* (1955) first discussed the structure of the problem and introduced quadratic cost approach. After a study of Holt *et al.* (1956) concentrated on the computational aspect of a model where a software was used to obtain results. The computational aspect is production planning accompanied with aspect of model which

calculates the amount to be produced, required number of worker, material to be place order. In simple word, all the information required to run a production. They found that the managers were going from one crisis to other with uncertain forecasts of frequent demand fluctuates for multiple products and huge fluctuations between overtime and idle time

Initially, APP was solved by quadratic programming but later it was remodeled so that linear programming (LP) technique can be applied to solve the problem. A standard LP model was developed for the APP. In the beginning fluctuations within demand is expected to be slower so the imprecise natures did not significantly affect the LP results. Later on, real situation forced consideration for demand fluctuations. Stochastic programming (SP) was used to solve the production problems. However, SP generally does not model real situation accurately as the approach does not provide any control to variability on solutions with different scenarios (Sadjadi 2011).

Regression analysis is used on managers' past performance to develop decision rules for aggregate planning as introduced by Bowman (1956). Bowman's work had far impact on operations management, particularly in artificial intelligence. He developed two heuristic rules, one for size of workforce and another for production rate, and tested both his model. Jones (1967) converted the HMMS (Holt, Modigliani, Muth and Simon's work) model into a 20 dimension response surface and used a search decision rule to find the solution. Taubert 1968 These are mathematics approach done in previous study of AP (Baykasoglu 2001) listed various studies on APP in the early years

- Trial and error method (Noori 1995)
- Search decision rule (Taubert 1968)
- Management's coefficients method (Bowman 1956)
- Production switching heuristic (Hing 1995)
- Transportation method (Bowman 1956)
- Goal programming (Abucanon 1985)

- Simulation models (Elkiri, 1996)

The objective of an APP may be single, dual or multiple in nature. In a single objective model, the minimization of the total cost function is usually the objective. This generally consists of production cost, inventory cost, shortage cost and cost of changes in labor level. In multi-objective models, the minimization of total cost is still the main objective, and the other objective is either maximization of service level, minimization of changes in work force level, or minimization of variability of total cost. A multi-objective plan is a combination of the single objective with two or more of the others.

Under general conditions, companies will likely face fluctuating demand. APP needs to find ways to minimize the related costs due to variation in demand and sales by adjusting production rates, workforce levels and inventory levels (Canel, 2013). The adjustments are carried out using a variety of operation research methods. There is a host of methods used to solve problems, but APP still remains a problem. Demand fluctuation not only affects the planning but also has an effect on the inventory level. A high inventory level leads to high aging on the inventory if there is no extra demand to absorb the product. In addition, planning for real situations needs to include effects of inflation. Physical shortages can occur unexpectedly and planners face difficulty in expediting on the next arrival of the material. Identifying the problem in early stages will prevent the issue from happening in the future. The process of identifying is shown step-by-step in Figure 1.1.

MOTIVATION

Imperfect production process happens due to equipment error and cannot be avoided during production process. Attrition is one of the imperfect production processes which cause the produced quantity is not produced as per planned by the planner. The situation causes consumption of raw material consumed earlier than expected and planner tends to order more raw material in advance which results in financial loss of the company. In some circumstances, the planner tends to have buffer stock which results in higher inventory holding cost on production floor. Therefore modifying an EPQ model and integrating it with APP model to enable planner to decide on lot size to run and resources required are necessary.



EXISTING WORK IN BOTH APP AND EPQ

EPQ	APP
The effect of imperfect process in EPQ leads to production of defective products. Recent modification done on EPQ model lead to optimal production quantity solution in shortage is allowed. But the solution does not solve the problem in overall.	The advantage of APP model is advance production planning and gives an idea to management for resources planning in situation on production demand which changes due to unexpected material shortage during production process. Thus, frequent revise in production planning is required.



LIMITATION

Existing inventory management systems do not consider attrition rate. Modification of EPQ model with inclusive of attrition rate. Two important models involve in production planning that are APP and EPQ were not linked together.



DESIRED SOLUTION

The role of demand of product is triggering all the cost in the industry. The material availability will ensure the production runs smoothly. This research therefore proposes a mathematical modelling to find optimal production quantity inclusive of attrition and based on the solution find the resources required to execute the production with shortage not allowed.

Figure 1.1 Flowchart of Problem Formulation

1.6 Problem Statement

For a production to run smoothly, a manufacturing company needs to have a proper production planning. However, it is difficult to plan production when the demand is deterministic. Attrition that happens during production adds to the fluctuation of the demand and produced defective products. If the attrition rate is not considered in the production planning, this may cause immediate physical shortage of the raw material and production may be interrupted and results in financial loss to the company. In order to overcome this problem, this research considers an Economic Production Quantity with Attrition (EPQA) model under deterministic demand assumption and, taking into account the attrition rate during the production with shortage not allowed, in finding the optimal production level. From the solution, the APP model will then be used to determine the resources required to meet the production level. In this work, the EPQA and APP models will be integrated.

1.7 Research Question

The problem statement raises several research challenges. These challenges will be addressed by providing answers to the following questions:

1. What are the roles of demand in production planning and what is the impact if physical shortages happen
 - i. What will be the impact to production when attrition happens in unexpected manner?
 - ii. How to prevent a production run from interruption?
 - iii. What is the solution to optimize finished goods rather than having extra buffer stock in production floor?

2. How can APP runs effectively under imperfect situation?
 - i. What is the production quantity for each product given that the production cost, inventory cost, worker's cost, hiring and firing cost and the cost varies within the planning period
 - ii. How to ensure the production runs minimum total production cost?
 - iii. What is the purpose of the both model integrated?

3. What is the impact when product cost, worker's cost, inventory varies?
 - i. What is the allowable increase of cost to minimize total production cost?
 - ii. How to ensure the varies of production costs does not impact number of quantity to be produced

1.8 Research Objective

The principal objective of this study is to develop a realistic integration of APP and EPQA for multiple product in multiple period to reduce the gap between existing literature and practical implementation. The specific objectives of the study have been identified as follows:

1. To analyze the demand behavior in situation of physical shortage that occurs due to attrition rate.
2. To determine the optimal lot size with attrition and no shortage is allowed using EPQA model
3. To determine the optimal production and resource level using APP model under EPQA demand assumption.
4. To investigate the effect of changes on the cost of parameters

1.9 Scope of the Research

The scope of the study is focused on the integration of EPQA and APP. This study will assume a situation of no shortage allowed, deterministic demand and imperfect process. The planning horizon will be 5 months. The investigation will be mainly on how to ensure no shortage even though in a situation of imperfect production process without revising the production planning due to material shortage.

1.10 Significance of the Research

EPQA is a model developed with one of the imperfect processes known as attrition. The model is mainly to obtain optimal lot size of production with known attrition quantity followed by APP model to find manufacturing resources. The integration of EPQA and APP benefits the production planner in advance planning based on the lot size inclusive of attrition and the required manufacturing resources.

1.11 Organization of Thesis

Chapter 1 introduces the research discipline, which is EPQ and APP for multi-product in multi-period. It also includes discussions of the problem background, problem statement, research objectives, significance as well as scope of the research.

Chapter 2 provides an extensive literature review of the study area. Extensive background work on the research discipline is also discussed here in addition to the chosen EPQ model, i.e. behavior of demand and APP model.

Chapter 3 discusses the procedure in conducting the research which include assumptions made, research design and procedure and operational framework.

Chapter 4 presents the development of the EPQ model with attrition and no shortage allowed. The model gives the economic production quantity and the total production cost.

Chapter 5 presents the development of APP Model under EPQ demand. The model is solved using LINGO 15.0. The solution presents number of workers required, the optimal production quantity and resources level in fulfilling the demand requirement for each period. The sensitivity analysis is carried out to find the effect of various production cost on the number of required workers. The reason is to find the minimum allowable changes of cost on which reflects change on number of workers.

In the final chapter, a summary of the entire research is done before concluding with the research findings. In addition, a few recommendations are also forwarded for future researches.

REFERENCE

- Bakir, Mehmet Akif. (1996). *A hybrid analytic/simulation modelling approach to production planning*. University of Nottingham.
- Baykasoglu, A. (2001). Moapps 1.0: *Aggregate production planning using the multiple-objective tabu search*. International Journal of Production Research, 39(16), 3685-3702.
- Bertsimas, Dimtris, & Thiele, Aurélie. (2006). *Robust and data-driven optimization: Modern decision-making under uncertainty*. INFORMS tutorials in operations research: models, methods, and applications for innovative decision making, 137.
- Billington, Peter J. (1987). *The classic economic production quantity model with setup cost as a function of capital expenditure**. Decision Sciences, 18(1), 25-42.
- Bowman, E. (1956). *Production planning by the transportation method of linear programming*. Journal of Operational Research Society, 100-103.
- Buscher, Udo, & Lindner, Gerd. (2007). *Optimizing a production system with rework and equal sized batch shipments*. Computers & Operations Research, 34(2), 515-535.
- Canel, L. D. (2013). *A comparison of mathematical programming techniques for aggregate production planning*. Journal of Interdisciplinary Mathematics, 266-274.
- Chan, WM, Ibrahim, RN, & Lochert, PB. (2003). *A new EPQ model: Integrating lower pricing, rework and reject situations*. Production Planning & Control, 14 (7), 588-595.
- Chiu, Yuanshyi Peter. (2003). *Determining the optimal lot size for the finite production model with random defective rate, the rework process, and backlogging*. Engineering Optimization, 35(4), 427-437.

Chung, Kun-Jen, Her, Chao-Chun, & Lin, Shy-Der. (2009). *A two-warehouse inventory model with imperfect quality production processes*. Computers & Industrial Engineering, 56(1), 193-197.

Ciarallo, Frank W, Akella, Ramakrishna, & Morton, Thomas E. (1994). *A periodic review, production planning model with uncertain capacity and uncertain demand optimality of extended myopic policies*. Management Science, 40(3), 320-332.

Crandall, Richard E. (1998). *Production planning in a variable demand environment*. Production and Inventory Management Journal, 39(4), 34.

Davenport, Thomas H. (1998). *Putting the enterprise into the enterprise system*. Harvard business review, 76(4).

Dorf, Richard C, & Kusiak, Andrew. (1994). *Handbook of design, manufacturing and automation*: Wiley Online Library.

Erdem, Asli Sencer, & Özekici, Süleyman. (2002). *Inventory models with random yield in a random environment*. International Journal of Production Economics, 78(3), 239-253.

Eroglu, Abdullah, & Ozdemir, Gultekin. (2007). *An economic order quantity model with defective items and shortages*. International journal of production economics, 106(2), 544-549.

Filho, OS Silva. (1999). *An aggregate production planning model with demand under uncertainty*. Production planning & control, 10(8), 745-756.

Foote, BL et al. (1988). *Production planning & scheduling: Computational feasibility of multi-criteria models of production, planning and scheduling*. Computers & Industrial Engineering, 15(1-4), 129-138.

Gardiner, Stanley C. (2002). *ERP and the reengineering of industrial marketing processes: A prescriptive overview for the new-age marketing manager*. Industrial Marketing Management, 31(4), 357-365.

Gore, George J. (1976). *Production/operations management*. Academy of Management Review, 1(2), 130-132.

Goyal, Suresh Kumar, & Cárdenas-Barrón, Leopoldo Eduardo. (2002). *Note on: Economic production quantity model for items with imperfect quality—a practical approach*. International Journal of Production Economics, 77(1), 85-87.

Hall, Robert W. (1983). *Zero inventories* Homewood. IL: Dow Jones-Irwin.

Hanssmann, Fred, & Hess, Sidney W. (1960). *A linear programming approach to production and employment scheduling*. Management science (1), 46-51.

Hayek, Pascale A, & Salameh, Moueen K. (2001). *Production lot sizing with the reworking of imperfect quality items produced*. Production Planning & Control, 12(6), 584-590.

Holt, Charles C, Modigliani, Franco, & Simon, Herbert A. (1955). *A linear decision rule for production and employment scheduling*. Management Science, 2(1), 1-30.

Hsu, Jia-Tzer, & Hsu, Lie-Fern. (2013b). *Two EPQ models with imperfect production processes, inspection errors, planned backorders, and sales returns*. Computers & Industrial Engineering, 64(1), 389-402.

Hsu, J. &. (2013). *Two EPQ models with imperfect production processes, inspection errors, planned backorder, and sales returns*. Computer and Industrial Engineering, 64(1), 389-402.

Hsu, L. F.-T. (2014). *Economic production quantity (EPQ) models under an imperfect production process with shortages backordered*. International Journal of System Science, 852-867.

Hwang*, Hark, & Cha, CN. (1995). *An improved version of the production switching heuristic for the aggregate production planning problem*. International journal of production research, 33(9), 2567-2577.

Inderfurth, Karl, & Vogelgesang, Stephanie. (2013). *Concepts for safety stock determination under stochastic demand and different types of random production yield*. European Journal of Operational Research, 224(2), 293-301.

- Jones, Curtis H. (1967). *Parametric production planning*. Management Science, 13(11), 843-866.
- Klaus, Helmut et al. (2000). *What is ERP?* Information systems frontiers, 2(2), 141-162.
- Kogan, K, & Portougal, V. (2006). *Multi-period aggregate production planning in a news-vendor framework*. Journal of the Operational Research Society, 423-433.
- Konstantaras, I, Goyal, SK, & Papachristos, Sotirios. (2007). *Economic ordering policy for an item with imperfect quality subject to the in-house inspection*. International Journal of Systems Science, 38(6), 473-482.
- Lee, William B, & Khumawala, Basheer M. (1974). *Simulation testing of aggregate production planning models in an implementation methodology*. Management Science, 20(6), 903-911.
- Liao, Gwo-Liang, & Sheu, Shey-Huei. (2011). *Economic production quantity model for randomly failing production process with minimal repair and imperfect maintenance*. International Journal of Production Economics, 130(1), 118-124.
- Maddah, Bacer, & Jaber, Mohamad Y. (2008). *Economic order quantity for items with imperfect quality: Revisited*. International Journal of Production Economics, 112(2), 808-815.
- Masud, Abu SM, & Hwang, CL. (1980). *An aggregate production planning model and application of three multiple objective decision methods†*. International Journal of Production Research, 18(6), 741-752.
- Mazzola, Joseph B et al. (1998). *Multiproduct production planning in the presence of work-force learning*. European Journal of Operational Research, 106(2), 336-356.
- Mirzapour Al-e-Hashem, SMJ, Baboli, A, Sadjadi, SJ, & Aryanezhad, MB. (2011). *A multiobjective stochastic production-distribution planning problem in an uncertain environment considering risk and workers productivity*. Mathematical Problems in Engineering, 2011

Nahmias, Steven, & Cheng, Ye. (2009). *Production and operations analysis* (Vol. 6): McGraw-Hill New York.

Noori, Hamid, & Radford, Russell W. (1995). *Production and operations management: Total quality and responsiveness*: McGraw-Hill New York.

Ouyang, LY, Chen, Cheng-Kang, & Chang, HC. (1999). *Lead time and ordering cost reductions in continuous review inventory systems with partial backorders*. Journal of the Operational Research Society, 50(12), 1272-1279.

Papachristos, S, & Konstantaras, I. (2006). *Economic ordering quantity models for items with imperfect quality*. International Journal of Production Economics, 100(1), 148-154.

Porkka, P et al. (2003). *Multiperiod production planning carrying over set-up time*. International Journal of Production Research, 41(6), 1133-1148.

Porteus, Evan L. (1986). *Optimal lot sizing, process quality improvement and setup cost reduction*. Operations research, 34(1), 137-144.

Raafat, Fred. (1991). *Survey of literature on continuously deteriorating inventory models*. Journal of the Operational Research society, 27-37.

Ravindran.A. (2008). *Operation Research And Management Science*. New York:Taylor & Francis Group.

Rosen, L Drew, & Canel, Cem. (2008). *A comparison of mathematical programming techniques for aggregate production planning*. Journal of Interdisciplinary Mathematics, 11(2), 266-274.

Sadjadi. S.M-e-H (2011) An efficient algorithm to solve a multi-objective robust aggregate production planning in an uncertain environment , *Springer*, 765- 782

Salameh, MK, & Jaber, (2000). *Economic production quantity model for items with imperfect quality*. International journal of production economics, 64(1), 59-64.

Sarker, Bhaba R, & Coates, Eyler Robert. (1997). *Manufacturing setup cost reduction under variable lead times and finite opportunities for investment*. International Journal of Production Economics, 49(3), 237-247.

Shafer, Scott M. (1991). *A spreadsheet approach to aggregate scheduling*. Production and Inventory Management Journal, 32(4), 4.

Shingo, Shigeo. (1985). *A revolution in manufacturing: The SMED system: Productivity Press*.

Stephen. (2004). *A robust optimization model for stochastic aggregate production planning*. Production planning & control, 15(5), 502-514.

Tabucanon, MT, & Mukyangkoon, S. (1985). *Multi-objective microcomputer-based interactive production planning*. International journal of production research, 23(5), 1001-1023.

Taft, E. W. (1918). *The most economical production lot*. Iron Age, 101(18), 1410-1412.

Taleizadeh et al. (2010). *Multi-product production quantity model with repair failure and partial backordering*. Computers & Industrial Engineering, 59(1), 45-54

Tang, L., Liu, J., Rong, A., & Yang, Z. (2001). *A review of planning and scheduling systems and methods for integrated steel production*. European Journal of Operational Research, 133(1), 1-20

Taubert, W.H. (1968) Search decision rule for the aggregate scheduling problem. *Management Science*, 343-359

Tersine, Richard J. (1994). *Principles of inventory and materials management*.

Vazsonyi, Andrew. (1956). *Operations research in production control-a progress report*. Operations Research, 4(1), 19-31.

Vollmann, Thomas E, Berry, William L, Whybark, D Clay, & Jacobs, F Robert. (2005). *Manufacturing planning and control for supply chain management*: McGraw-Hill/Irwin New York.

Vroom, Victor. (1964). *Expectancy theory of motivation. Management study guide* [Online]available at: <http://www.managementstudyguide.com/expectancy>. [Accessed 3 December 2010].

Wee, Hui M, Yu, Jonas, & Chen, Mei C. (2007). *Optimal inventory model for items with imperfect quality and shortage backordering*. Omega, 35(1), 7-11.

Yano, Candace Arai, & Lee, Hau L. (1995). *Lot sizing with random yields: A review*. Operations Research, 43(2), 311-334.

Zacks, Shelemyahu. (1998). *Modern industrial statistics: Design and control of quality and reliability*: Cengage Learning.

Zimmermann, H-J. (2000). *An application-oriented view of modelling uncertainty*. European Journal of operational research, 122(2), 190-198.